Intelligent Data Analysis
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## Exercise Sheet 7

Exercise 24 Decision Trees: Attribute Selection Measures
Compute the information gain and the $\chi^{2}$ measure for the following two contingency tables, which refer to two descriptive attributes $A, B$ and one class attribute $C$ !

|  | $A$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | $a_{1}$ | $a_{2}$ | $a_{3}$ |  |
|  | $c_{1}$ | 9 | 4 | 3 |
| $C$ | $c_{2}$ | 3 | 9 | 4 |
|  | $c_{3}$ | 4 | 3 | 9 |


|  | $B$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | $b_{1}$ | $b_{2}$ | $b_{3}$ |
|  | $c_{1}$ | 9 | 4 | 3 |
| $C$ | $c_{2}$ | 6 | 6 | 4 |
|  | $c_{3}$ | 1 | 6 | 9 |

How may one describe the selection behavior of the two measures intuitively? (Hint: Mind the first row and the last column of the two tables.)

Exercise 25 Decision Trees: Pruning
Prune the following decision tree using the approach of pessimistic pruning! (parameter: 0.5 additional errors)


## Exercise $26 \quad c$-Means Clustering

Consider the following two-dimensional data set:

| $x$ | 1 | 6 | 8 | 3 | 2 | 2 | 6 | 6 | 7 | 7 | 8 | 8 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | 5 | 2 | 1 | 5 | 4 | 6 | 1 | 8 | 3 | 6 | 3 | 7 |

Process this data set with $c$-means clustering with $c=3$ (i.e., try to find 3 clusters)! Use the first three data tuples als initial positions for the cluster centers and observe the migration of the centers.

## Exercise $27 \quad c$-Means Clustering

In exercises 16 and 17 on sheet 7 we considered a simple two-dimensional data set. Reconsider this data set, but assume that that no class information is available for the data points. That is, consider the following data set:

| $x$ | 3 | 3 | 4 | 4 | 5 | 6 | 7 | 7 | 8 | 9 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $y$ | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 6 | 5 | 7 | 3 | 4 | 5 | 6 | 6 | 7 | 8 | 8 | 8 | 9 |

a) Which problem of c-means clustering becomes obvious when this data set is processed with $c=2$ (i.e., if one tries to find two clusters)?
Hint: What is the desired result? What is produced by c-means clustering?
(You need not compute the exact result of the algorithm, a qualitative description suffices. Compare the result to a naive Bayes classifier.)
b) How could one try to cope with this problem?

Hint: Recall what distinguishes a full and a naive Bayes classifier.

## Additional Exercise Lagrange Theory

Determine the minimum of the function $f(x, y)=x y^{2}+x+2 y$ under the constraints $x y=1$ and $x>0$ with the help of the method of Lagrange multipliers!

