# Exercise Sheet 10

## **Exercise 31** *c*-Means Clustering

Consider the following two-dimensional data set:

| x | 1 | 6 | 8 | 3 | 2 | 2 | 6 | 6 | 7 | 7 | 8 | 8 |
|---|---|---|---|---|---|---|---|---|---|---|---|---|
| y | 5 | 2 | 1 | 5 | 4 | 6 | 1 | 8 | 3 | 6 | 3 | 7 |

Process this data set with c-means clustering with c = 3 (i.e., try to find 3 clusters)! Use the first three data tuples als initial positions for the cluster centers and observe the migration of the centers.

#### **Exercise 32** *c*-Means Clustering

In exercises 21 and 22 on sheet 7 we considered a simple two-dimensional data set. Reconsider this data set, but assume that that no class information is available for the data points. That is, consider the following data set:

| x | 3 | 3 | 4 | 4 | 5 | 6 | 7 | 7 | 8 | 9 | 1 | 2 | 2 | 3 | 4 | 5 | 5 | 6 | 7 | 7 |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| y | 1 | 2 | 2 | 3 | 3 | 4 | 4 | 6 | 5 | 7 | 3 | 4 | 5 | 6 | 6 | 7 | 8 | 8 | 8 | 9 |

a) Which problem of c-means clustering becomes obvious when this data set is processed with c = 2 (i.e., if one tries to find two clusters)? Hint: What is the desired result? What is produced by c-means clustering? (You need not compute the exact result of the algorithm, a qualitative description suffices. Compare the result to a naive Bayes classifier.)

b) How could one try to cope with this problem?Hint: Recall what distinguishes a full and a naive Bayes classifier.

## **Exercise 33** Fuzzy Clustering

Consider the one-dimensional data set

We want to process this data set with fuzzy c-means clustering with c = 2 (two clusters) and a fuzzifier of w = 2. Assume that the cluster centers are initialized to 1 and 5. Execute one step of alternating optimization as it is used for fuzzy clustering, i.e.:

- a) Compute the membership degrees of the data points for the initial cluster centers!
- b) Compute new cluster centers from the membership degrees computed in this way!

## **Exercise 34** Expectation Maximization

Consider again the one-dimensional data set used in exercise 33, which we want to process in this exercise with the expectation maximization algorithm to estimate the parameters of a mixture of two normal/Gaussian distributions. Let the prior probabilities of the two clusters be fixed to  $\theta_i = \frac{1}{2}$  and the variances to  $\sigma_i^2 = 1$ , i = 1, 2. (That is, only the expected values of the normal distributions — the cluster centers — are to be adapted.) Use the same values for the initial cluster centers as in exercise 40, that is, 1 and 5. Compute one expectation step and one maximization step, i.e.:

- a) Compute the posterior probabilities of the data points for the initial cluster centers!
- b) Estimate new cluster centers from the data point weights computed in this way!