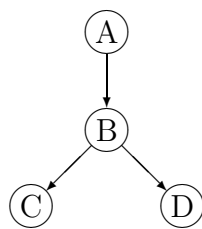


**Exercise Sheet 7**

**Exercise 22** Probabilistic Propagation

Consider the following Bayesian network and the corresponding (conditional) probability distributions:



$P(A)$	$a_1$	$a_2$
	0.4	0.6

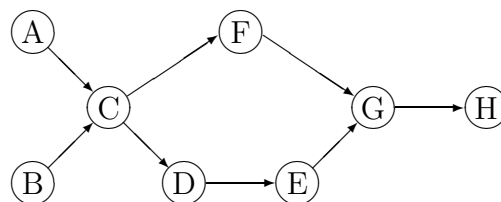
$P(B A)$	$a_1$	$a_2$
$b_1$	0.1	0.6
$b_2$	0.9	0.4

$P(C B)$	$b_1$	$b_2$
$c_1$	0.4	0.8
$c_2$	0.6	0.2

$P(D B)$	$b_1$	$b_2$
$d_1$	0.7	0.2
$d_2$	0.3	0.8

- Determine the a-priori distribution for all four variables!
- It becomes evident that variable  $C$  assumes value  $c_2$ . Propagate this evidence across the network with the tree-based propagation algorithm presented in the lecture, i.e., compute all four a-posteriori distributions!

**Exercise 23** Construction of Clique Trees



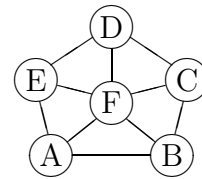
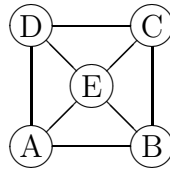
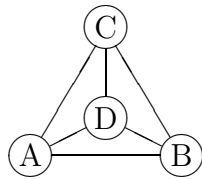
Construct stepwise for the depicted Bayesian network

- the moral graph,
- a triangulated moral graph, and
- a cliquen tree/join tree!

At which steps of the construction do you have multiple options to proceed?

**Exercise 24**      Triangulation and Joint Tree Construction

Given the following three undirected graphs:



- a) Check which graphs are triangulated! Try to recognize this without applying the triangulation algorithm from the lecture.
- b) Triangulate the graphs that are not yet triangulated and determine for each of them a join tree!