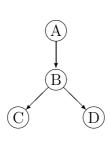
## Exercise Sheet 6

## Exercise 19 Probabilistic Propagation

Consider the following Bayesian network and the corresponding (conditional) probability distributions:



P(A)	$a_1$	$a_2$
	0.4	0.6

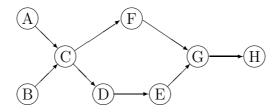
P(C B)	$b_1$	$b_2$
$c_1$	0.4	0.8
$c_2$	0.6	0.2

P(B A)	$a_1$	$a_2$
$b_1$	0.1	0.6
$b_2$	0.9	0.4

P(D B)	$b_1$	$b_2$
$d_1$	0.7	0.2
$d_2$	0.3	0.8

- a) Determine the a-priori distribution for all four variables!
- b) It becomes evident that variable C assumes value  $c_2$ . Propagate this evidence across the network with the tree-based propagation algorithm presented in the lecture, i.e., compute all four a-posteriori distributions!

## Exercise 20 Construction of Clique Trees



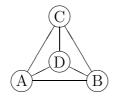
Construct stepwise for the depicted Bayesian network

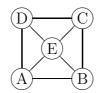
- a) the moral graph,
- b) a triangulated moral graph, and
- c) a cliquen tree/join tree!

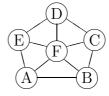
At which steps of the construction do you have multiple options to proceed?

## Exercise 21 Triangulation and Joint Tree Construction

Given the following three undirected graphs:







- a) Check which graphs are triangulated! Try to recognize this without applying the triangulation algorithm from the lecture.
- b) Triangulate the graphs that are not yet triangulated and determine for each of them a join tree!